

Here are some integrals to practice on. Before computing any of the integrals, decide which methods will be used: substitution, integration by parts, partial fractions, trig substitution.

Compute the following integrals. If the integral is improper, determine whether it converges or diverges. If an improper integral converges, find its value.

$$1. \int_0^1 x^3(x^4 - 1)^5 dx$$

$$2. \int \frac{2}{\sqrt{9-4x^2}} dx$$

$$3. \int \frac{x}{9-4x^2} dx$$

$$4. \int \frac{2x}{(x-1)(x+2)} dx$$

$$5. \int_0^1 x^2 e^{2x} dx$$

$$6. \int_0^{\pi/2} e^{\cos x} \sin x dx$$

$$7. \int_{1/2}^1 \cos(\pi x) \sin^3(\pi x) dx$$

$$8. \int \frac{1+\sqrt{t}}{\sqrt{t}} dt$$

$$9. \int x e^{-4x} dx$$

$$10. \int_0^{\infty} x e^{-4x} dx$$

$$11. \int_0^e \frac{\ln x}{x} dx$$

12. $\int_0^{\pi/4} \cos 2x \sqrt{\sin 2x} \, dx$

13. Prove the formula $\int \tan x \, dx = -\ln|\cos x| + C$. Hint: $\tan x = \frac{\sin x}{\cos x}$

14. Find the area of the region bounded by the curve $y = \frac{x}{x^2 - 1}$ and the x -axis between $x = 0$ and $x = \frac{1}{2}$ using three different methods: substitution, partial fractions, and trig substitution.